

IMPACTS OF NARROWBAND INTERFERENCE ON OFDM-UWB RECEIVERS: ANALYSIS AND MITIGATION

**Kai Shi et al., IEEE Transactions on Signal Processing, Vol. 55, No. 3,
March 2007**

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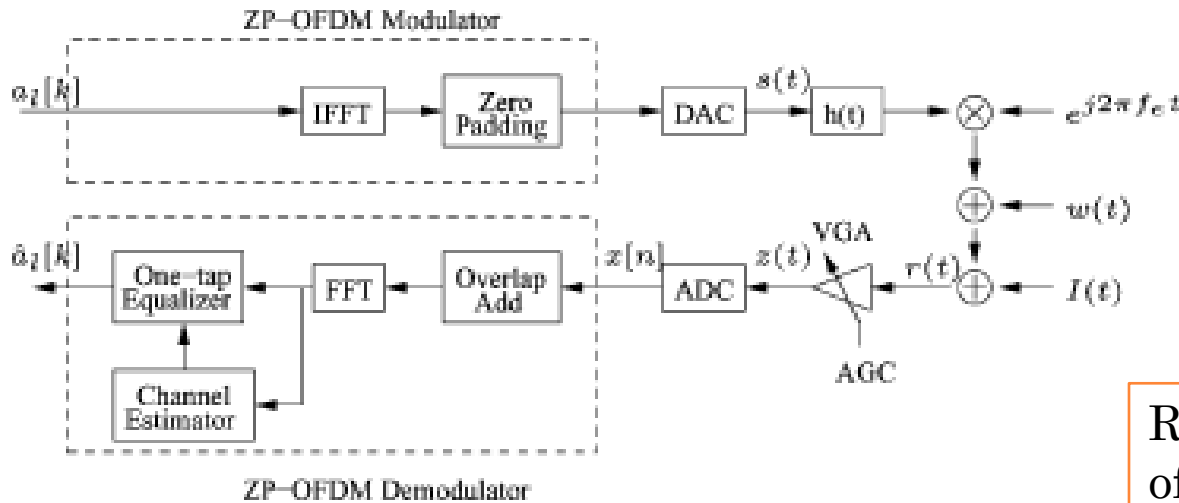
INTRODUCTION

- The transmitted power level of UWB is limited to -41.3 dBm/MHz and can be spread over a huge BW 7.5 GHz .
- Enables the coexistence with other services such as GPS, IEEE 802.11 WLANs, IEEE 802.16 WiMax, etc.
- Due to their low Tx power and huge reception BW, **UWB systems are subjected to NBIs.**
- The scope of this paper is to analyze the **impacts of NBI on the performance of an OFDM-UWB receiver.**

INTRODUCTION

- This doc presents an in-depth analysis of the **impact of NBI on SINR loss at the O/P of ADC**.
- **Importance?** SINR at the O/P of ADC serves as a good metric to evaluate the uncoded BER performance of an OFDM-UWB Rx.
- It is found that NBI increases the level of quantization noise.
- **Solution?** higher precision ADC. However, UWB receivers employs a flash data converter!
 - Proposed? **Mixed interference mitigation scheme.**

SIGNAL MODEL



Rectangular pulse of duration T_0

Subcarrier spacing

QPSK data

The transmitted signal

$$s(t) = \frac{1}{\sqrt{KT}} \sum_I \sum_{k \in C} a_l[k] e^{j2\pi k(t - IT_0)/T} g(t - IT_0)$$

Number of data subcarriers

Set of data subcarriers

SIGNAL MODEL

The power of the transmitted symbols is normalized to unity:

$$E[|a_l[k]|^2], E[|s(t)|^2] = 1$$

- A discrete-time implementation of $s(t)$ that assumes the **sampling period** $T_s = T/N$ is generated by means of N -point IFFT.
- According to CLT, $s[n] := s(nT_s)$ can be approximated as a complex **Gaussian RV** for sufficiently large number of subcarriers $N \geq 20$.
- In addition, OFDM modulation assumes a ZP of length $T_g = N_g T_s$ at the end of each symbol instead of CP.
- The above model is only fit for the conventional SB-OFDM systems. It is still applicable to the baseband of transceiver for both SB-OFDM and MB-OFDM.

SIGNAL MODEL

The received signal can be expressed by:

$$r(t) = e^{j2\pi f_c t} [s(t) \otimes h(t)] + w(t) + I(t)$$

CFO
 CIR
 Thermal noise
 NBI

The NBI is modeled by a linearly modulated signal of the form:

$$I(t) = A_i \sum_n b_n e^{j(2\pi f_i t + \Phi_i)} p(t - nT_i)$$

Modulated symbols
of the interference
 Rectangular pulse
 Symbol period

IMPACTS OF NBI ON DATA CONVERTERS

- Due to the channel fading, the **received** signal $r(t)$ presents a very large dynamic range.
- To improve the efficiency of the finite precision ADC, a **VGA** is used to normalize the power level to a desired level.
- The normalized signal $z(t)$ is next **sampled** by ADC $z[n]=z(nT_s)$ and **quantized** into the digital signal $x[n]$.
- For simplicity, a complex baseband model is used hereafter, and all signals are expressed in discrete time domain.
- Next the **performance of ADC** will be analyzed for two channel conditions: **without and with NBI**.

IMPACTS OF NBI ON DATA CONVERTERS

○ A. NBI Free Channel

The received signal:

$$r[n] = e^{j2\pi un} \sum_{m=0}^{M-1} s[n-m]h[m] + w[n]$$

$f_e T_s$, normalized CFO

AWGN and variance: $\sigma_n^2 = E\{|w[n]|^2\}$

Assume a **quasi-static channel model with M paths** and instantaneous channel power:

$$\sigma_c^{-2} = \sum_{m=0}^{M-1} |h[n]|^2$$

Therefore, the instantaneous power $r[n]$ is given by:

$$\sigma_r^2 = \sigma_c^{-2} + \sigma_n^2$$

IMPACTS OF NBI ON DATA CONVERTERS

If σ_z^2 is denoted as the **instantaneous power of VGA O/P** $z[n]$, i.e., $\sigma_z^2 = |z[n]|^2$.
The VGA O/P becomes $z[n]=G.r[n]$, where $G = \sqrt{\sigma_z^2 / \sigma_r^2}$.

If the maximum quantization level of ADC is 1, the **PAPR of ADC** can be defined as (?)

$$\Omega = \frac{1}{\sigma_z^2/2}$$

To achieve a sampling speed as high as 528 MHz in OFDM-UWB Rx, a low-bit uniform ADC appears as the best solution. For a uniform b-bit ADC, the **quantization step size**:

$$\Delta = \frac{2}{2^b - 1}$$

The **power of the complex quantization noise** $q[n] := x[n] - z[n]$

$$\sigma_q^2 = 4 \sum_{i=0}^{2^{b-1}-2} \int_{i\Delta}^{(i+1)\Delta} (z - (i + 1/2)\Delta)^2 p(z) dz$$

$$+ 4 \int_{1-\Delta/2}^{\infty} (z - 1)^2 p(z) dz$$

pdf of I and Q components of $z[n]$

IMPACTS OF NBI ON DATA CONVERTERS

- Since both $s[n]$ and $w[n]$ can be interpreted as CGRVs, we can view $z[n]$ as CGRV in AWGN channel.
- UWB MP channel is modeled by a multi-cluster quasi-static channel with large M ($M > 15$). Although the paths within each cluster are correlated, the simulated histogram shows that the Gaussian approximation of $z[n]$ still holds.
- Therefore, given b and σ_z^2 , one can easily calculate the quantization noise power σ_q^2 .
- The signal-to-quantization-noise ratio: $\gamma_q = \frac{\sigma_z^2}{\sigma_q^2}$.
- For a given b , the optimum Ω can be found by solving

$$\partial \gamma_q / \partial \Omega = 0$$

IMPACTS OF NBI ON DATA CONVERTERS

- For a specific b-bit ADC, there is a optimum PAPR

ADC bit number	Optimum Ω (dB)	Best γ_q (dB)
4	8.0	19.4
5	9.3	24.6
6	10.3	29.8

- Higher precision ADCs lead to larger PAPR and higher Ω and higher γ_q
- For ADC O/P $x[n]$, the SNR is given by,

$$\text{SNR}_x = \frac{G^2 \bar{\sigma}_c^2}{\sigma_q^2 + G^2 \sigma_n^2}.$$

- Ignoring OLA and assuming perfect Synch

$$X[k] = \text{FFT}(z[n] + q[n]) = G(a[k]H[k] + W[k]) + Q[k],$$

IMPACTS OF NBI ON DATA CONVERTERS

- According to CLT, $Q[k]$ can be modeled as a GRV. Therefore, $X[k]$ can be viewed as GRV, as well.
- After some direct manipulations,

$$\text{SNR}_x = \frac{\bar{\sigma}_c^2}{(\bar{\sigma}_c^2 + \sigma_n^2) / \gamma_q + \sigma_n^2} \longrightarrow A$$

- This can be used to evaluate the uncoded BER of OFDM receiver.

IMPACTS OF NBI ON DATA CONVERTERS

- B. NBI Channel
- The received signal becomes

$$r[n] = e^{j2\pi un} \sum_{m=0}^{M-1} s[n-m]h[m] + I[n] + w[n]$$

NBI with average power σ_i^2

- The ADC O/P is given by:

$$x[n] = G \left(e^{j2\pi un} \sum_{m=0}^{M-1} s[n-m]h[m] + w[n] + I[n] \right) + q[n].$$

- SINR of $x[n]$:

$$\text{SINR}_x = \frac{G^2 \bar{\sigma}_c^2}{\sigma_q^2 + G^2 (\sigma_n^2 + \sigma_i^2)} \quad \longrightarrow \quad \text{C}$$

- And,

$$\text{SINR}_x = \frac{\bar{\sigma}_c^2}{(\bar{\sigma}_c^2 + \sigma_n^2 + \sigma_i^2) / \gamma_q + \sigma_n^2 + \sigma_i^2} \quad \longrightarrow \quad \text{B}$$

IMPACTS OF NBI ON DATA CONVERTERS

- Comparing (A) and (B), we find that NBI introduces two effects:

$$\text{SNR}_x = \frac{\bar{\sigma}_c^2}{(\bar{\sigma}_c^2 + \sigma_n^2) / \gamma_q + \sigma_n^2}$$



A

$$\text{SINR}_x = \frac{\bar{\sigma}_c^2}{(\bar{\sigma}_c^2 + \sigma_n^2 + \sigma_i^2) / \gamma_q + \sigma_n^2 + \sigma_i^2}$$



B

- The increase of received signal power leads to a smaller gain G for VGA, which causes the larger quantization noise:

$$\sigma_q^2 / G^2 = (\bar{\sigma}_c^2 + \sigma_n^2 + \sigma_i^2) / \gamma_q \quad \longleftarrow \quad G = \sqrt{\sigma_z^2 / \sigma_r^2}$$

- As to the third term of denominator in (B), interference directly affects the tone of $\text{Int}(f_i T_s)$ and its neighbor tones.

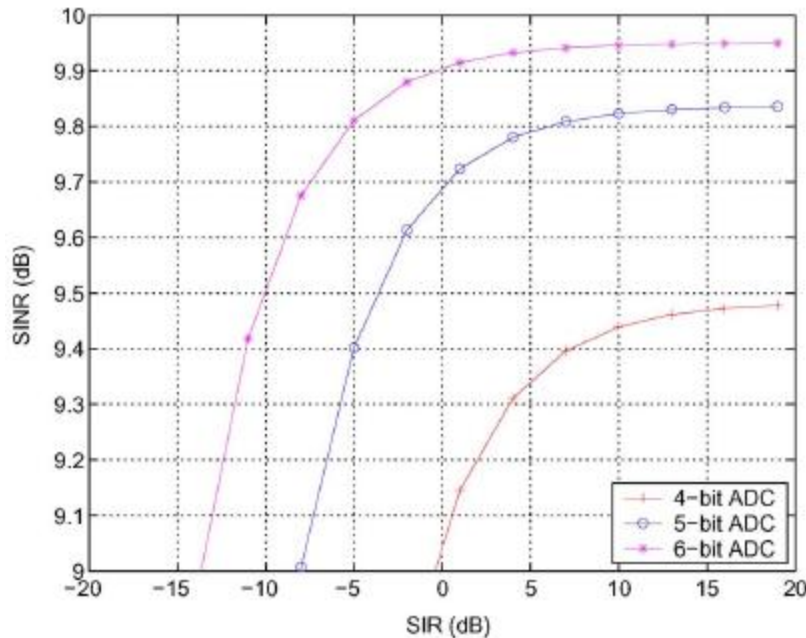
IMPACTS OF NBI ON DATA CONVERTERS

- We focus on the **first effect of NBI**, the enlarged quantization noise. Omitting the third term of denominator in (C),

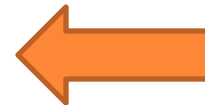
$$\text{SINR}_x = \frac{\bar{\sigma}_e^2}{(\bar{\sigma}_e^2 + \sigma_n^2 + \sigma_i^2) / \gamma_q + \sigma_n^2} \quad \longrightarrow \quad \mathbf{D}$$

- Assuming the same optimum value for γ_q as the one given by previous table and denoting $\boxed{\text{SIR} = \bar{\sigma}_e^2 / \sigma_i^2}$ as the SIR of $r(t)$, we **compare the SINR curves of ADC**.

IMPACTS OF NBI ON DATA CONVERTERS



$$\bar{\sigma}_e^2 / \sigma_n^2 = 10 \text{ dB.}$$



Signal to thermal noise ratio

- As the NBI becomes stronger, the SINR of ADC is reduced.
- Ex. Reducing the SIR from 20 to 0 dB results in 0.5 dB SINR loss for the 4-bit ADC.

NBI SUPPRESSION


- When compared to the desired WB signal, the interference occupies a much smaller frequency band and presents a higher PSD.
- This motivates us to use **transform-domain filtering** techniques to suppress the NBI.
 - TD→FD, find frequency location, frequency excision, remaining signal FD→TD.

A. Digital NBI detection and mitigation

- Since the phase of the NBI is unknown, the **NBI has to be detected noncoherently** based on the absolute values of the received signal samples.
- The highest peak corresponds to the subcarrier affected by NBI

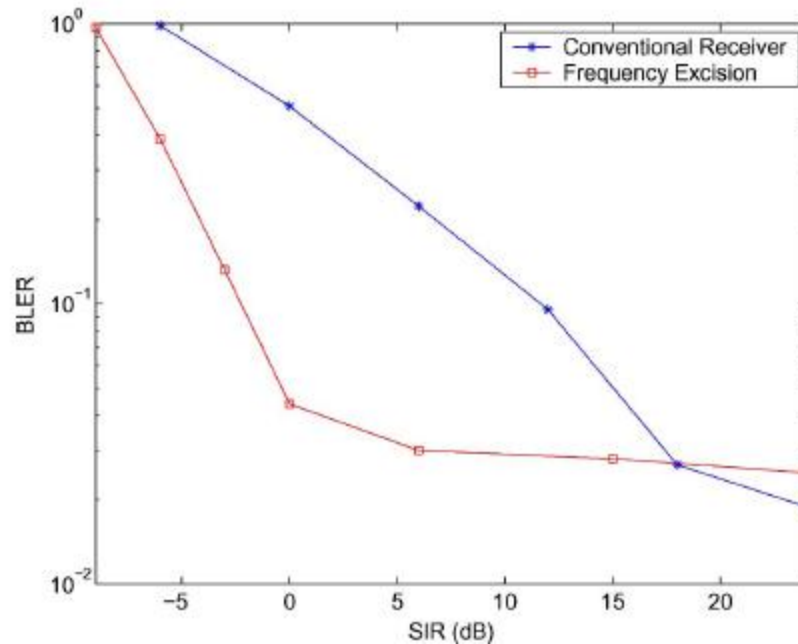
NBI SUPPRESSION

$$|X[k]|^2$$

- By comparing the magnitude-squared of the FFT bins with a threshold T_h , we can find the existence and location of NBI.
- Lost data caused by excision can be recovered by channel decoding techniques.
- Four adjacent subcarriers are also excised. (Why?)
- We observe the BLER plots 

NBI SUPPRESSION

- Conventional means no frequency excision



$$\sigma_{\text{I}}^2 / \sigma_{\text{N}}^2 = 6 \text{ dB.}$$

- To achieve BLER=0.05, the conventional receiver requires SIR=15 dB. However, Rx with freq. excision needs 0 dB.

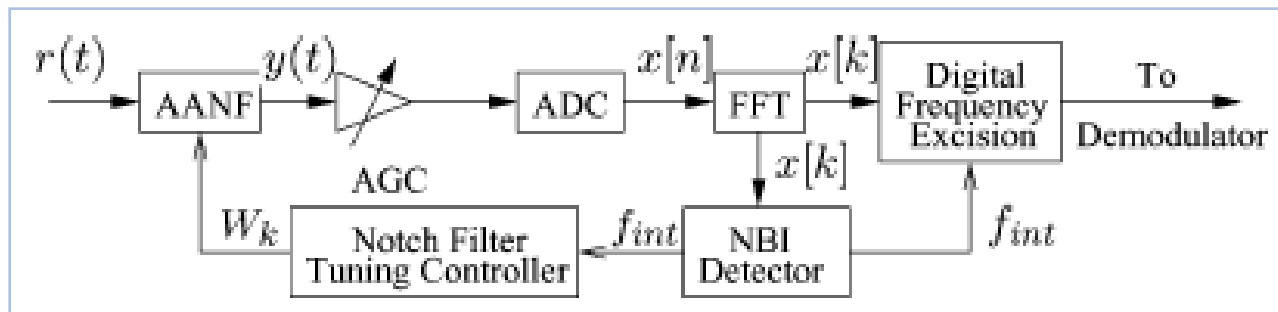
NBI SUPPRESSION

- As the SIR decrease, the BLER of Rx w. freq. excision increase very rapidly. (why?)
 - As NBI becomes stronger, normalized quantization noise σ_q^2/G^2 is increased, which leads to the SINR loss (D).
 - With the increasing power of NBI, spectral leakage becomes worse (more power of NBI will be leaked to the neighboring subcarriers).
- Possible solutions? **Increasing the number of bits of ADC.**
Drawback → not affordable for practical UWB Rx.
 - Alternate? To suppress strong NBI, we need to find a low-complexity scheme.

NBI SUPPRESSION

B. Analog NBI Cancellation:

- Freq. excision method can not remedy the performance degradation when $SIR < 0 \text{ dB}$.
 - The gain of the VGA is set according to the power of NBI, effectively increasing the quantization noise of the ADC.
 - Logical solution? **Remove NBI before it enters the AGC and ADC.**
- New suppression scheme: **adaptive analog noise filter (AANF)** with notch freq. f_0 .

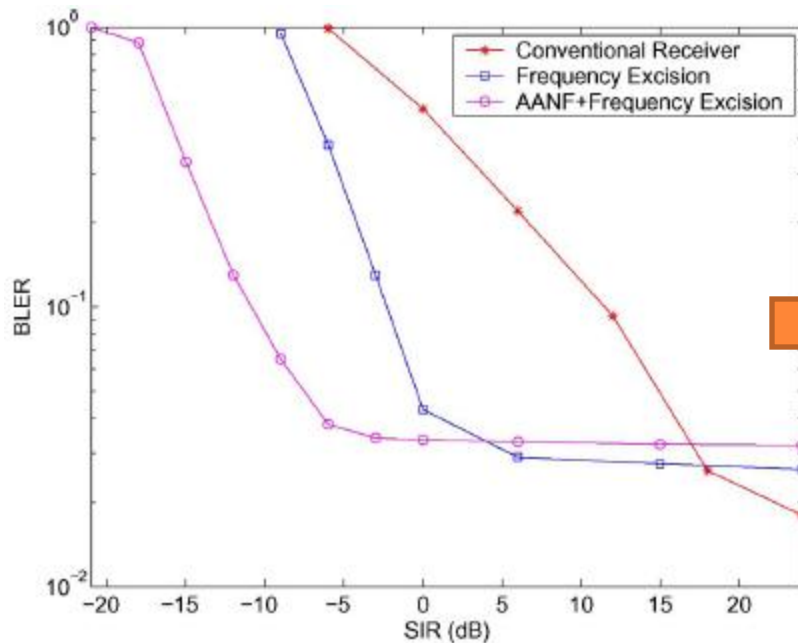


NBI SUPPRESSION

- For weak NBI level, freq. excision method is sufficient. However, for significant NBI, AANF needs to be activated.
- By controlling the notch frequency f_0 , the contaminated freq. component is removed before it goes into AGC.
- To combat NBI adaptively, the AANF should be designed to be tunable in the whole reception BW.
- For MB-OFDM, BW of one sub-band is 528 MHz spread from -264 to 264 MHz.

NBI SUPPRESSION

C. Performance of mixed NBI suppression scheme



For example, to achieve $BLER=0.1$,

1. the Rx with digital freq. excision needs $SIR > -3 \text{ dB}$.

2. While mixed scheme can allow SIR as low as -12 dB .

- At $SIR > 0 \text{ dB}$, there is a crossover (?)
 - Bypass AANF at $SIR > 0 \text{ dB}$.

CONCLUSION

- An in-depth study to assess the impact of NBI on the operation of ADC.
- Optimized designing of AGC can not remedy the performance loss at high NBI level.
- Most of the NBI have focused on purely digital cancellation
 - Not viable solution for MB-OFDM UWB systems
- **Mixed NBI suppression scheme is proposed.**

Thanks for your cooperation

Questions/Comments